Fine-grained crowd distribution forecasting with multi-order spatial interactions using mobile phone data

Mingxiao Li\textsuperscript{a,h,c}, Song Gao\textsuperscript{b,}\*, Peiyuan Qiu\textsuperscript{c,d}, Wei Tu\textsuperscript{a}, Feng Lu\textsuperscript{c,e,f}, Tianhong Zhao\textsuperscript{a}, Qingquan Li\textsuperscript{a}

\textsuperscript{a} Guangdong Key Laboratory of Urban Informatics, Shenzhen Key Laboratory of Spatial Information Smart Sensing and Services, and Research Institute of Smart Cities, School of Architecture & Urban Planning, Shenzhen University, Shenzhen 518060, China
\textsuperscript{b} Geospatial Data Science Lab, Department of Geography, University of Wisconsin, Madison, WI 53706, USA
\textsuperscript{c} State Key Laboratory of Resources and Environmental Information System, Institute of Geographic Sciences and Natural Resources Research, Chinese Academy of Sciences, Beijing 100101, China
\textsuperscript{d} College of Surveying and Geo-Informatics, Shandong Jiansu University, Jinan 250101, China
\textsuperscript{e} University of Chinese Academy of Sciences, Beijing 100049, China
\textsuperscript{f} The Academy of Digital China, Fuzhou University, Fuzhou 350002, China

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ABSTRACT

Fine-grained crowd distribution forecasting benefits smart transportation operations and management, such as public transport dispatch, traffic demand prediction, and transport emergency response. Considering the co-evolutionary patterns of crowd distribution, the interactions among places are essential for modelling crowd distribution variations. However, two issues remain. First, the lack of sampling design in passive big data acquisition makes the spatial interaction characterizations of less crowded places insufficient. Second, the multi-order spatial interactions among places can help forecasting crowd distribution but are rarely considered in the existing literature. To address these issues, a novel crowd distribution forecasting method with multi-order spatial interactions was proposed. In particular, a weighted random walk algorithm was applied to generate simulated trajectories for improving the interaction characterizations derived from sparse mobile phone data. The multi-order spatial interactions among contextual non-adjacent places were modelled with an embedding learning technique. The future crowd distribution was forecasted via a graph-based deep neural network. The proposed method was verified using a real-world mobile phone dataset, and the results showed that both the multi-order spatial interactions and the trajectory data enhancement algorithm helped improve the crowd distribution forecasting performance. The proposed method can be utilized for capturing fine-grained crowd distribution, which supports various applications such as intelligent transportation management and public health decision making.

* Corresponding author.
E-mail address: song.gao@wisc.edu (S. Gao).

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1. Introduction

Fine-grained spatiotemporal crowd distribution forecasting is essential for traffic governance, urban management, and public health (Huang et al., 2021; Li et al., 2019a-c; Xu et al., 2018; Yao et al., 2020). For example, the department of traffic management can reschedule public transportation based on dynamic population distribution forecasting results to improve public travel efficiency; emergency management departments can forecast the crowd gathering processes of urban mass events, thereby improving the scientific nature and timeliness of control measures to reduce the risk of trampling (Chen et al., 2020; Iacobucci et al., 2019; Wang et al., 2019; Yuan & Raubal, 2016). Accurate crowd distribution forecasting can provide technical support and a decision-making basis for solving transportation problems and facilitating fine-grained traffic management, which is of great significance to the development of smart transportation.

Due to the lack of effective observation techniques, traditional urban mobility studies are mainly based on survey data, which limits the representativeness and spatiotemporal coverage of these studies (Zhang & Zhu, 2018; Chen et al., 2016). With the development of mobile positioning technology and the ubiquity of smart devices, long-time large-volume individual tracking data provide alternative opportunities for capturing the variation in human activities (Li et al., 2020; Yang et al., 2019; Gao et al., 2015; Gonzalez et al., 2008). In addition, breakthroughs in trajectory data mining and machine learning provide methodological support for urban mobility studies and applications (Ke et al., 2021; Liu et al., 2019; Park et al., 2019). They highlight the necessity of crowd distribution inference and forecasting (Li et al., 2021; Mimura et al., 2019; Chen et al., 2018).

With reference to the existing research on crowd distribution forecasting, two issues remain. First, the lack of sampling design in passive big data acquisition limits the accuracy and the stability of spatial interaction modelling. That is, the extracted spatial interaction pattern may significantly vary due to different sampling strategies and spatial heterogeneity in data distribution. This phenomenon is particularly evident in the less crowded places, which lead to the data hungry problem (Li et al., 2019; Yang et al., 2019). An example is shown in Fig. 1. Assuming that $P_d$ is a place having 200 individuals at present, of which 130 individuals also stay in $P_d$ at the previous time period moment and other 15, 50, and 5 individuals come from $P_a$, $P_b$, $P_c$, respectively. When the data were randomly sampled at 10% of the population in each place, it may have resulted in oversampling of the individuals staying at $P_d$, while $P_a$ and $P_c$, which originally had interactions with $P_d$, showed no interaction. This makes the spatial interaction characterizations of less crowded places insufficient, thereby reducing the accuracy of crowd distribution forecasting.

Second, the interactions among places cause crowd distribution variations, and these interactions can be reflected in individual movement trajectories (Peng et al., 2019; Zhu et al., 2018; Liu et al., 2017). The individual movement trajectories among multiple places portray the processes of crowd gathering and dispersing. These processes can be regarded as the multi-order spatial interactions among different places at the aggregation level. As far as we know, existing crowd forecasting studies often generalize trajectories as series of first-order interactions between two anchor places (origin-destination (OD) flows), thus ignoring the multi-order spatial interaction processes among the places (Li et al., 2021; Zhu et al. 2020). However, crowd distribution variation is influenced not only by contextual adjacent places (first-order interaction) but also by contextual non-adjacent places (multi-order interactions). For example, when one travels from home to work via a bus stop, if the entire movement trajectory is generalized and divided into the interaction between home and bus stop and the interaction between bus stop and work, the important multi-order/multi-context interactions between home and work will be ignored (Crivellari & Beinat 2019). Researches on multi-order spatial interaction learning can help model spatial correlations more comprehensively, thus improving the accuracy and interpretability of crowd distribution forecasting.

To address these issues, we proposed a novel Crowd Distribution Forecasting method with Multi-order Spatial Interaction, called CDF-MSI, to forecast future crowd spatiotemporal distribution. The main contributions of this study are summarized as follows:

1. A trajectory enhancement algorithm was applied to mitigate the problem of inaccurate interaction modelling in less crowded places caused by the lack of sampling design.
2. The multi-order spatial interactions among contextual non-adjacent places were considered in the crowd distribution forecasting modelling to improve the forecasting accuracy and stability.
3. A crowd distribution forecasting model was constructed using a hybrid graph-based deep neural network for modelling the spatiotemporal patterns of crowd distribution with multi-order spatial interactions.

![Fig. 1. An illustration of the spatial interaction pattern variation caused by data sampling.](image-url)
(4) The performance of the proposed CDF-MSI method was evaluated with a real-world mobile phone dataset in Senegal. The results demonstrated the superiority of our proposed method over other baseline approaches.

The remaining parts of this paper are organized as follows. Section 2 presents a literature review on crowd distribution forecasting and its related studies. Section 3 presents the details of our proposed CDF-MSI method. Section 4 presents the experimental results and the performance analysis of the case study. Section 5 discusses the broad implications of this work and our vision for future work. Finally, Section 6 presents the conclusion of this study.

2. Literature review

2.1. Future crowd distribution forecasting

The urgent demand for forecasting future crowd distribution in applications such as public transport scheduling, emergency dispatch, mobile communication, and base station operations has promoted the development of crowd distribution forecasting research. According to the different aspects of attention, the existing methods can be divided into two categories: temporal variation pattern-based forecasting methods and spatial interaction pattern-based forecasting methods (Panczak et al., 2020).

Temporal variation pattern-based methods forecast future crowd distribution by modelling the temporal tendency and periodicity of the given crowd distribution time sequence (Cecaj et al., 2020; Cheng et al., 2020; Mimura et al., 2019; Li et al., 2012). For example, Xue et al. (2020) proposed an expression method to reasonably divide a region and time period to determine the crowd distribution statistics and then designed an improved long short-term memory (LSTM) network to forecast future crowd distribution based on the temporal proximity, periodicity and trend characteristics. Mimura et al. (2019) designed a time series generation model based on conditional variational autoencoders and an LSTM network. It forecasts future crowd distribution by analysing the temporal variations in crowd distribution series and the influence of weather factors. Liang et al. (2016) designed a computational forecasting framework with parallel flow based on RNNs, which can effectively forecast near real-time crowd distribution by analysing the sequence characteristics of crowd size variations in a specific region. However, these methods only mine patterns from the historical time series of crowd distribution and ignore the effects of spatial interactions and spatial correlations, thus limiting their forecasting performance across space (Zhen et al., 2019; Shaw and Yu, 2009).

To address previous issues, researchers have started to forecast future crowd distribution by modelling the spatial interaction characteristics among places (Li et al., 2021; Crivellari & Beinat, 2019; Crols & Malleson, 2019; Chen et al., 2018). For example, Crols & Malleson (2019) applied a multi-agent model to characterize the commuting behaviours contained in travel survey data, thereby forecasting the crowd distribution by calibrating the difference between the distributions of commuters and urban populations based on Wi-Fi data. Chen et al. (2018) designed an artificial neural network to express the relationships between a historical crowd distribution and the inflow and outflow of people in each neighbourhood and forecasted the future crowd distribution in a large metropolitan area. On the basis of crowd movement behaviours in physical space, Li et al. (2021) integrated the interactions in physical spaces and social spaces with a graph fusion technique and forecasted the future crowd distribution by combining a GCN and an LSTM. However, most of the existing studies only consider first-order interaction characteristics (e.g., physical distances and OD flows) as the impact factors of crowd distribution forecasting. This makes the developed models fail to measure the influence of multi-order spatial interactions among contextual non-adjacent places on crowd distribution, resulting in insufficient forecasting accuracy and interpretability.

It is worth noting that the superiority of deep learning methods in capturing complex non-linear relationships has made it widely used in the field of traffic forecasting, such as traffic demand forecasting (Ke et al., 2021; Jin et al., 2020; Xu et al., 2017), traffic flow forecasting (Xu et al., 2022; Zhu et al., 2020; Zhang et al., 2020; Qiu et al., 2020), and traffic condition forecasting (Medrano & Aznarte, 2021; Zheng et al., 2020; Cui et al., 2019). For example, Ke et al. (2021) proposed a multi-task & graph learning approach to enable the knowledge of multiple kinds of service modes sharing across networks and designed various multi-graph convolutional networks for forecasting ride demands for different service modes. Zhang et al. (2020) regarded a road network as graphs for considering the topological structure of the underlying network and applied a GCN to forecast short-term traffic conditions. Geng et al. (2019) proposed a spatiotemporal multi-graph convolution network to capture the complicated spatiotemporal dependencies among different places and forecasted ride-hailing demand using a multi-graph integrated convolution technique. Li et al. (2017) designed a diffusion convolutional recurrent network for traffic flow forecasting by capturing the spatiotemporal dependency of traffic flows using bi-directional graph random walk and recurrent neural network with scheduled sampling. Solutions to these similar spatio-temporal forecasting problems provide reference and methodological foundation for crowd distribution forecasting. How to integrate deep learning methods and domain knowledge to improve the performance of crowd distribution forecasting is still a challenging problem worth exploring.

2.2. Historical crowd distribution mapping

The mapping of historical crowd distribution is the basis of crowd forecasting studies. Depending on the data sources used, the existing crowd distribution mapping methods can be divided into natural and socioeconomic data-based mapping methods, remote sensing image-based mapping methods, and geotagged data-based mapping methods.

The main idea of natural and socioeconomic data-based mapping methods is to quantitatively analyse the relationships between relevant factors and crowd distribution variations, thus assigning coarse-grained census data to fine-grained space (Leasure et al.,
Although this type of method has good spatial coverage and can improve the spatial granularity of crowd distribution mapping to a certain extent, it suffers from the problems of lagging data and a long update period. In addition, when combining natural and socioeconomic data with census data, problems such as temporal mismatches and inconsistencies across multiple statistical metrics affect the accuracy of crowd distribution mapping results.

Remote sensing image-based mapping methods mainly extract the features of relevant elements affecting crowd distribution through remote sensing images to establish relationships between the corresponding elements and crowd distribution variations. Common elements include the night-time lighting index, built-up area, etc. (You et al., 2020; Georganos et al., 2019). For example, Xing et al. (2020) proposed a deep learning architecture for learning the physical characteristics of remote sensing images and integrated neighbour effects to improve the crowd distribution mapping performance. Stathakis et al. (2018) assumed that the variations in observed night lights were a valid proxy for crowd distribution, thus estimating season-specific ambient crowd counts in Greece. This type of model significantly improves the spatial granularity and timeliness of prediction, but the acquisition of remote sensing data is limited by the given satellite transit time and weather conditions. This makes the mapping results of these methods unable to capture the dynamic processes of fine-grained population distributions (e.g., hourly) and suffers from missing data problems.

With the decreasing data collection cost, the geotagged data-based mapping method has become mainstream in historical crowd distribution mapping. Emerging methods focus on taxi trajectories, social media data or smart card data (Hara et al., 2020; Hipp et al., 2018; Wang et al., 2018). However, the sample biases in these data make the mapping results suffer from representativeness problems (Mellon & Prosser, 2017). Since mobile phone data cover almost all classes of the population and have fine spatiotemporal granularity, they have become one of the main data sources for historical crowd distribution mapping (Salat et al., 2020; Li et al., 2020; Liu et al., 2018; Deville et al., 2014). Kang et al. (2012) quantitatively analysed the correlations among the number of calls, the number of active mobile phone users, and the size of the associated crowd, thus demonstrating the linear relationships between crowd distribution and mobile phone indicators. Cheng et al. (2020) mapped monthly crowd distribution across China using mobile phone data and environmental ancillary data through a hybrid method containing a random forest model and area-to-point interpolation. The importance measures of the explanatory variables in this hybrid method demonstrated the ascendency of mobile phone data in crowd distribution mapping. However, since most mobile phone data only record the corresponding location when communication or transition behaviour occurs, mobile phone data suffer from the data sparsity problem (Li et al., 2019; Chen et al., 2019). In addition, the lack of corresponding attribute values (e.g., age, gender, etc.) in mobile phone data limits the application of crowd distribution mapping results to a certain extent.

### 2.3. Spatial interaction pattern analysis

Spatial interaction refers to the phenomenon of the movement or exchange of people, objects or information that occurs among places (Tobler, 1976). It reveals the connections among places, which provides great support for research on crowd distribution variation (Ullman, 1953; Park et al., 2018).

Limited by data availability, traditional spatial interaction intensity estimation methods mostly regard places as nodes and construct mechanistic models to estimate spatial interaction intensity. The most common models include the gravity model, intervening opportunities model, and random walk model. For example, the gravity model draws on the idea of the law of gravity, which suggests that the intensity of spatial interaction is proportional to regional attributes (population, gross domestic product, etc.) and decays with increasing inter-regional distance (Zipf, 1946). The gravity model is widely used in many fields, such as population migration and international trade; however, it has certain shortcomings in practical applications due to its reliance on historical data calibration for parameter setting and the need for a priori knowledge to perform distance function selection (Gupta et al., 2019; Park et al., 2018). The intervening opportunities model introduced the principle of maximum entropy instead of spatial distance to explain spatial interaction intensity, which reflects the decision processes of human travel behaviours in the original hypothesis (Stouffer, 1940). However, this model has problems such as an overcomplicated solution process and the underestimation of long-distance travel proportions. Simini et al. (2012) regarded a spatial interaction as a random process determined by a joint probability, which was determined by the crowd distribution of the origin, destination and calculation radius. This model makes it possible to estimate spatial interaction intensities by only inputting the crowd distribution, thereby solving the cold start problem of spatial interaction intensity estimation models.

Different from the above mechanistic model, the quick accumulation of geotagged data enables us to estimate and forecast the intensities of the spatial interactions among places from a data-driven perspective (Ouyang et al., 2020; Wu et al., 2018). For example, Zhang et al. (2017) designed a deep spatio-temporal residual network (ST-ResNet) to forecast spatial interaction intensities by modelling the spatial dependence and the proximity, periodicity, and trend characteristics of the input spatial interaction intensity sequences. Wu et al. (2018) introduced an attention mechanism based on convolutional and RNN models by automatically learning the historical importance of spatial interaction intensities to further improve the accuracy of spatial forecasting. It is worth noting that the generation of spatial interactions is related to the selection of human movement behaviours, and this selection process is directly reflected in human movement trajectories (Zhang et al., 2021; Liu et al., 2020). The learning of interaction patterns among multiple places based on trajectory data will help us understand the mechanisms of human movement behaviours, measure the spatial correlations among places more comprehensively, and then improve the accuracy and interpretability of crowd distribution forecasting.

### 3. Methodology

The details of our proposed crowd distribution forecasting method are presented in this section. It contains three parts. First, the
3. Trajectory data enhancement

Due to the lack of sampling design in passive trajectory data acquisition, the extracted spatial interaction pattern may significantly vary. This makes the spatial interaction characterizations of less crowded places especially insufficient, thereby reducing the accuracy of crowd distribution forecasting. To mitigate this issue, a weighted random walk algorithm was used to generate simulated trajectories which started at less crowded places for trajectory data enhancement.

To minimize the difference between the simulated trajectories and real trajectories, we represent the interaction patterns reflected in the input historical trajectories as a directed and weighted graph for trajectory simulation. In this graph, the places were represented as nodes, and the number of interaction records between two places was taken as the edge weight. An illustration of the interaction graph is shown in Fig. 3, where $w_{ij}$ represents the number of interaction records from a place $S_i$ to another $S_j$, and an interaction was detected when the two adjacent trajectory records of one individual were linked to different places.

Combined with the generated interaction graph, trajectory simulation can be regarded as a weighted random walk process. In this study, a second-order random walk algorithm was introduced for trajectory data enhancement (Grover & Leskovec, 2016). Different from the simple weighted random walk algorithm that simulates the next visit place based on the current place $S_t$ and the edge weight $w_{ij}$, our second-order algorithm also considered the effects of the previously visited place $S_{t-1}$ to further minimize the difference between the simulated trajectories and real trajectories. The simulation process can be briefly explained as follows. Given the current place $S_m$ and the previously visited place $S_l$ that an agent has visited, the probability of visiting the next place $S_n$ can be defined as

$$P(S_n|S_m, S_l) = \frac{w_{mn}}{\sum_{S_n'} w_{S_m'S_n'}}$$

Fig. 2. The overall framework of the CDF-MSI method.
follows:

\[
P(\text{Sl+1} = \text{Sn}|\text{Sl} = \text{Sm}) = \alpha(l,n)^*w_{m,n}/Z
\]

(1)

\[
\alpha(l,n) = \begin{cases} 
1/p, & \text{if } d_{l,n} = 0 \\
1, & \text{if } d_{l,n} = 1 \\
1/q, & \text{if } d_{l,n} = 2 
\end{cases}
\]

(2)

where \( P \) indicates the visit probability, \( w_{m,n} \) indicates the corresponding edge weight in the interaction graph, \( Z \) indicates the standardized coefficients, and \( d_{l,n} \) indicates the minimum number of edges between places \( \text{Sl} \) and \( \text{Sn} \). Parameter \( p \) controls the likelihood of revisiting nodes in the walk, and a high value of this parameter ensures a lower probability of visiting a visited place; parameter \( q \) controls the search to move in the “inward” or “outward” direction, and a high value of this parameter ensures a lower probability of visiting places close to \( \text{Sl} \). The parameters \( p \) and \( q \) can be calibrated based on the movement pattern of the real trajectories which were tuned as 0.25 and 2 in this case study. Based on the proposed weighted random walk algorithm, the less crowded places were chosen as start nodes, and simulated trajectories were generated for trajectory data enhancement. The generated simulation trajectories and the real trajectories will be used as inputs for subsequent multi-order spatial interaction learning together to enhance the effectiveness of spatial interaction characterization. It is worth noting that the generated simulation trajectories in less crowded places were only used for learning the spatial interaction pattern among places (i.e., the underlying connectivity and spatial structure of places) and were not used in the crowd distribution estimation. The crowd distribution was only obtained from the real trajectories.

3.2. Multi-order spatial interaction learning

The movements of individuals among different locations/places can cause crowd distribution variations. As a microscopic part of an urban system, the individual movement behaviours recorded in the trajectory data provide a feasible idea for measuring the multi-order spatial interaction characteristics of places. Inspired by the achievements in computational linguistics, we regarded the trajectories as text sequences, thereby introducing an embedding learning technique to characterize the multi-order interactions among places (Zhang et al., 2021).

As the word2vec model can effectively extract the co-occurrence relationships and common context relationships among words in text, it has become a popular embedding learning technique. The core idea of this model is to express words as \( N \)-dimensional vectors and make a vector of words with more co-occurrences and common context relationships that are more similar. Therefore, the semantic relevance among words can be measured through vector similarity. Considering the data structure similarity between trajectory and text sequences, we used this model to characterize the multi-order interactions among places. An illustration of the places

(a) S1 → S2 → S3 → S4
(b) S1 → S3 → S4

Fig. 3. An illustration of interaction graph generation.

\[ G_T = \begin{bmatrix}
0 & 40 & 18 & 0 & 0 \\
25 & 0 & 35 & 108 & 0 \\
26 & 0 & 77 & 0 & 64 \\
0 & 23 & 46 & 0 & 64 \\
0 & 82 & 0 & 72 & 0
\end{bmatrix} \]

Fig. 4. An illustration of places that (a) share a common context or (b) frequently co-occur. The places labelled in blue have high spatial correlations. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
with common context and co-occurrence relationships is shown in Fig. 4. As shown in Fig. 4(a), the places $S_2$, $S_3$, and $S_4$ have common upstream and downstream neighbours $S_1$ and $S_5$, indicating that these places have common context relationships. Correspondingly, the places $S_3$ and $S_4$ in Fig. 4(b) appear in two trajectory segments $\langle S_1, S_3, S_4 \rangle$ and $\langle S_2, S_3, S_4 \rangle$, indicating that these places have co-occurrence relationships. The places with either common context or co-occurrence relationships have high spatial correlations, thus justifying the usage of the word2vec model for multi-order spatial interaction learning.

The training process can be briefly summarized as follows. Given an enhanced trajectory $\text{Traj}_k = S_1, S_2, \ldots, S_H$, the core idea is to maximize the average log probability:

$$\frac{1}{H} \sum_{h=1}^{H} \sum_{k=1}^{K} \log P(S_{t+k} | S_t)$$

where $K$ indicates the number of spatial interaction orders considered in the model. $P(S_{t+k} | S_t)$ indicates the probability of correctly forecasting visit place $S_{t+k}$ given current place $S_t$, and this probability is defined as follows:

$$P(S_{t+k} | S_t) = \frac{\exp(\langle u_{S_{t+k}} \rangle^T u_{S_t})}{\sum_{v=1}^{V} \exp(\langle u_{S_v} \rangle^T u_{S_t})}$$

where $V$ indicates the number of places and $u_{S_v}$ and $u_{S_t}$ indicate the initial one-hot vector and the trained $N$-dimensional vector of the place, respectively. The training process typically uses the back-propagation rule (Rumelhart et al., 1986). More technical details can be found in the paper (Mikolov et al., 2013). It is worth noting that only trajectories from the training data were used to learn the multi-order spatial interaction to avoid overfitting phenomena.

With the trained model, each place can be expressed as an $N$-dimensional vector. Therefore, the multi-order spatial interaction graph can be calculated by the similarity between each pair of trained vectors as follows:

$$\text{MSI}_{(i,j)} = \frac{u_{S_i} \cdot u_{S_j}}{\|u_{S_i}\| \cdot \|u_{S_j}\|}$$

where $\text{MSI}_{(i,j)}$ indicates the multi-order spatial interaction strength between places $S_i$ and $S_j$, and $\|u_{S_i}\|$ and $\|u_{S_j}\|$ represent the norms of trained vectors $u_{S_i}$ and $u_{S_j}$, respectively. A higher $\text{MSI}_{(i,j)}$ value indicates that the two places more frequently co-occur or share common contexts in the trajectories, that is, a higher multi-order interaction strength between the two places.

### 3.3. Forecasting model with a graph-based deep neural network

Based on the multi-order spatial interaction graph, a graph-based deep neural network model was designed for crowd distribution forecasting. The architecture of this model can be summarized in two parts: the characterization of the multi-order spatial interaction pattern of the crowd distribution with a GCN module and the characterization of the temporal variation pattern of the crowd distribution with an RNN module. An illustration of the CDF-MSI model is shown in Fig. 4.

As shown in Fig. 5, the current crowd distribution $Cd_t$ and the multi-order spatial interaction matrix $\text{MSI}$ were first organized into graph form as the model input. Specifically, the places were abstracted as nodes, the crowd distribution $Cd_t$ was abstracted as node weights, and $\text{MSI}$ was abstracted as edge weights. It is worth noting that the $\text{MSI}$ matrix should be transformed into a Laplacian matrix.
Examples of individual trajectory data extracted from call detail records.

The spatial variation pattern of the crowd distribution, which can be calculated as follows:

\[ C_d^{t+1} = \epsilon (MSI * C_d^t * W^r) \]  

where \( C_d^t \) represents the feature matrix (which equals \( C_d \) when the number of convolutions \( r \) equals one), \( \epsilon \) represents the activation function, \( MSI \) represents the multi-order spatial interaction matrix \( MSI \) changed by the Laplace transform, and \( W^r \) represents the weight matrix for model training.

On the basis of the GCN module, an RNN module was then used as the encoding–decoding framework for modelling the temporal variation pattern of the crowd distribution. During this process, a time step \( T \) was first determined with the temporal autocorrelation function (Cheng et al., 2020). According to the determined time step, the feature matrices \( C_d^{t+1}, C_d^{t+2}, \ldots, C_d^{t+T} \) were organized into time series and inputted into the RNN module. An LSTM architecture was used in our method and the corresponding formulas are shown as follows:

\[ z_t^r = \sigma (W^r [C_d^{t+1}, h^{t-1}] + b^r) \]  

\[ \tilde{C}_t = \tanh (W^r [C_d^{t+1}, h^{t-1}] + b^r) \]  

\[ C_t = z_t^r \odot \tilde{C}_t + z_t^r \odot \tilde{C}_t \]  

\[ h_t = z_t^r \odot \tanh (C_t) \]

where \( C_d^{t+1} \) represents the trained result of GCN module, \( z_t^r \) represents the gate state at time \( t \), \( g \in \{ f, i, o \} \) indicate the forget gate, input gate, and output gate, respectively. \( C_t \) and \( h_t \) represent the cell state and the current output at time \( t \). \( \tilde{C}_t \) represents the candidate values that could be added to cell state. \( W^r \) and \( W_t \) represent the corresponding weight matrix, and \( b^r \) and \( b_t \) represent the corresponding bias. The minimum root mean square error (RMSE) of the forecasted crowd distribution was used as the optimization criterion for model training. With this architecture, the CDF-MSI model was trained to forecast future crowd distribution. When performing forecasting, the new crowd distribution matrix sequence and the multi-order spatial interaction strength matrix were passed into the trained model, and then the forecasting results of the crowd distribution were obtained.

4. Case study

4.1. Data and experiment setup

The data used in this study were obtained from an anonymized mobile phone dataset provided by a major telecom operator in Senegal. It contains over 300,000 of individuals for one year in 2013. The dataset was accessed through the “Data for Development” challenge (De Montjoye et al. 2014). The data we used were the individual trajectories extracted from the call detail records of 10% of the sampled users. An example from this dataset is shown in Table 1. It is worth noting that all personal information was deleted before the data were provided due to personal privacy concerns. The data whose numbers of active days were preferred to be deleted in the data pre-processing. Accordingly, as the number of users was generally linearly proportional to the size of the crowd (Kang et al., 2012), the catchment area of the cell phone tower was regarded as the place.

The parameters used in this case study are shown in Table 2. The parameters were mainly tuned according to the grid search strategy based on the lowest obtained RMSE value on the validation dataset (Chai et al., 2018). The simulated trajectory length was tuned to 22, which corresponded to the weekly average length of the real individual trajectories. The less crowded places in this paper were defined as the places with the total crowd count in the bottom 20% of all places. It was inspired by the Pareto principle (Sanders, 1987), and the specific value was 48 in this study. The less crowded places were chosen as start nodes for trajectory data enhancement until the average count of individuals in this place reached the less crowded threshold. The spaces of parameters can be calibrated based on the individual movement pattern and the crowd distribution pattern (Li et al., 2020).

<table>
<thead>
<tr>
<th>Individual ID</th>
<th>Date</th>
<th>Time</th>
<th>Tower ID</th>
<th>Longitude</th>
<th>Latitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>4607****</td>
<td>01-07</td>
<td>020</td>
<td>164</td>
<td>−17.45**</td>
<td>14.74**</td>
</tr>
<tr>
<td>4607****</td>
<td>01-07</td>
<td>10:10</td>
<td>88</td>
<td>−17.46**</td>
<td>14.74**</td>
</tr>
<tr>
<td>4607****</td>
<td>01-07</td>
<td>10:50</td>
<td>134</td>
<td>−17.46**</td>
<td>14.75**</td>
</tr>
<tr>
<td>4607****</td>
<td>01-20</td>
<td>21:10</td>
<td>143</td>
<td>−17.45**</td>
<td>14.74**</td>
</tr>
</tbody>
</table>

Table 1 Examples of individual trajectory data extracted from call detail records.
4.2. Evaluation metrics

The RMSE, MAE and StDev metrics were used to evaluate the forecasting errors and the stability of the forecasting methods. Given the crowd distribution of all cell phone towers at time $t C_t = c_{t1}, c_{t2}, \ldots, c_{tV}$ and the forecasted crowd distribution $\hat{C}_t = \hat{c}_{t1}, \hat{c}_{t2}, \ldots, \hat{c}_{tV}$, the evaluation metrics can be defined as follows:

$$RMSE = \sqrt{\frac{\sum_{t=1}^{T} \frac{1}{V} \sum_{v=1}^{V} (c_{tv} - \hat{c}_{tv})^2}{V^*T}}$$  \hspace{1cm} (11)

$$MAE = \frac{\sum_{t=1}^{T} \frac{1}{V} \sum_{v=1}^{V} |c_{tv} - \hat{c}_{tv}|}{V^*T}$$  \hspace{1cm} (12)

$$StDev = \sqrt{\frac{\sum_{t=1}^{T} \frac{1}{V} \sum_{v=1}^{V} (c_{tv} - \hat{c}_{tv})^2 - \text{Error}^2}{V^*T - 1}}$$  \hspace{1cm} (13)
where \( V \) represents the number of cell phone towers, \( T \) represents the number of time slots needed to be forecasted, and \( \text{Error} \) represents the average of all forecasting errors. The maps of the average forecasting performance (RMSE and MAE) and forecasting error deviation (StDev) with respect to each place are shown in Fig. 7.

4.3. Comparison of the CDF-MSI method with baselines

To evaluate the performance of our proposed CDF-MSI method relative to that existing crowd distribution forecasting methods using machine learning, the following five methods were selected as baselines. For all methods, the parameters were tuned with a grid search algorithm based on the performance on the validation dataset. The detailed parameters of baselines were attached in Table S1 in the supplement file. To test the stability of the forecasting performance, each method was run ten times repeatedly. The average of ten results was used to indicate the average predictive performance of each model, and the best result of each method was used for subsequent analysis.

- **Spatio-Temporal meta-Model (STMeta):** This model integrated generalizable spatiotemporal knowledge with multi-view learning and predicted the crowd flows by combining graph convolution LSTM and attention mechanism (Wang et al., 2020).
- **Diffusion Convolutional Recurrent Neural Network (DCRNN):** This model captured the spatiotemporal dependency of traffic flows by using bi-directional graph random walk and recurrent neural network with scheduled sampling (Li et al., 2017).
- **Attention based Spatial-Temporal GCN (ASTGCN):** This model applied a spatiotemporal attention mechanism to model the autocorrelations within the crowd distribution and capture the spatiotemporal variation patterns by combining a GCN and a standard convolutional network (Guo et al., 2019).
- **LSTM:** This model is one of the most advanced recurrent deep learning techniques used in time series data modelling. It has been widely used in similar forecasting tasks such as traffic flow forecasting and next location forecasting. (Ren et al., 2020; Li et al., 2020).
- **K-Nearest Neighbours (KNN):** This model splits the crowd distribution sequences into fixed-length sub-sequences and finds the \( k \) samples that are most similar to the forecasted sequence. The average value or weighted average value of the \( k \) samples was outputted as the forecasting result (Smith et al., 2002).
- **Gradient-Boosting Decision Tree (GBDT):** The GBDT model regards fixed-length crowd distribution sub-sequences as features and trains a model with an iterative decision tree generation algorithm. The results of all trained decision trees are added as the forecasting result (Friedman, 2001).

The comparison results are shown in Table 3. The best RMSE and MAE of our proposed CDF-MSI method were 8.885 and 4.633, respectively, thus outperforming all other baseline methods. The StDev of the CDF-MSI method was also the lowest, indicating that our proposed method showed an advantage regarding the stability of the forecasting error. Considering the sensitivity of the RMSE to outliers, the RMSE was used as the major evaluation metric in subsequent analysis (Chai & Draxler, 2014). We observed that the deep learning-based methods, including CDF-MSI, STMeta, DCRNN, ASTGCN, and LSTM, outperformed the classical machine learning-based methods. This phenomenon can be explained by the fact that deep learning-based methods better capture non-linear and complex spatiotemporal variation patterns. The spatiotemporal methods (CDF-MSI, STMeta, DCRNN, and the ASTGCN) showed better forecasting performance than the temporal methods (LSTM, KNN, and the GBDT), which may demonstrate the necessity of considering spatial patterns in the crowd distribution forecasting problem. It is worth noting that the RMSE and StDev values were not significantly different. This is mainly because some of the forecasting errors were positive and some were negative, making the average forecasting error \( \text{Error} \) (as shown in Formula 13) approximately equal to zero. However, these are two different aspects of the metrics used to evaluate the forecasting error and the stability of the forecasting error.

A significance test was further conducted to verify the significance of the forecasting performance differences between the CDF-MSI method and the other baseline methods. Considering that the forecasting errors did not conform to a Gaussian distribution, the Kolmogorov-Smirnov test (K-S test) was chosen as the indicator. As shown in Table 4, all compared pairs achieved larger K-S statistic values than the expected values of the null hypothesis, and the \( p \)-values were <0.001. The results indicate that the forecasting errors of CDF-MSI were significantly different from those of the other methods, thus demonstrating the effectiveness of our proposed method.

### Table 3

<table>
<thead>
<tr>
<th>Category</th>
<th>Method</th>
<th>RMSE Mean Best</th>
<th>MAE Mean Best</th>
<th>StDev Mean Best</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>STMeta</td>
<td>10.817 10.809</td>
<td>5.910 5.902</td>
<td>10.784 10.777</td>
</tr>
<tr>
<td></td>
<td>LSTM</td>
<td>29.462 29.458</td>
<td>4.907 4.880</td>
<td>29.450 29.446</td>
</tr>
<tr>
<td>Classical</td>
<td>GBDT</td>
<td>46.875 46.874</td>
<td>6.588 6.576</td>
<td>46.858 46.856</td>
</tr>
<tr>
<td>Machine Learning</td>
<td>KNN</td>
<td>47.241 47.241</td>
<td>7.141 7.141</td>
<td>47.222 47.222</td>
</tr>
</tbody>
</table>
To further demonstrate the advantage of our proposed CDF-MSI method, the forecasting performance was evaluated in terms of the size of the crowd and the diversity of the crowd variations. As discussed previously, the forecasting performance varies for places with different levels of congestion. With reference to Senegal’s urbanization rate of approximately 40%, we classified the places into three groups with crowd size thresholds of 195 and 435 (World Bank, 2014). The thresholds corresponded to cumulative distribution values of 60% and 90% with respect to the size of the crowd statistical distribution, roughly dividing the case study area into rural areas, township areas, and urban areas. The comparison results are shown in Fig. 8. We observed that the forecasting performance decreased with increasing crowd size. It was to be expected that the less crowded places led to simpler variation patterns and lower forecasting difficulty. Note that although the RMSE of our proposed CDF-MSI method increased from 4.647 to 16.620, it still achieved good performance among the compared methods.

The diversity of the crowd variations in the places affects the forecasting performance from another perspective. In this study, the standard deviation of the crowd size over the time series in a place was used to evaluate the stability and complexity of crowd size variations. Correspondingly, the division thresholds were chosen as 35 and 95, representing cumulative distribution values of 60% and 90%, respectively, in terms of the diversity of the statistical distribution of the crowd variations in places. The comparison results are shown in Fig. 9. All the comparison methods achieved good forecasting performance when the crowd variation diversity was simple. Note that the differences in forecasting performance between our proposed CDF-MSI method and the classical machine learning methods for both the small crowd size group and simple variation group were small. This result indicates that the complex methods tended to be more significantly improved when solving complex problems. Nevertheless, our method still performed well for each group.

### 4.4. Evaluation of the two algorithms in the CDF-MSI method

As mentioned in the methodology section, a trajectory enhancement algorithm and a multi-order spatial interaction learning algorithm were applied in the CDF-MSI method to achieve forecasting performance improvement. To verify the applicability of these two algorithms on performance improvement, three strategies were designed for performance evaluation: (1) models with the trajectory enhancement part and the multi-order spatial interaction learning (with suffix -MSI), (2) models with the multi-order spatial interaction learning algorithm only (with suffix -OMSI), and (3) models with the first-order interaction as edge weights only (with suffix -FI). In addition, to verify the applicability of these two algorithms on performance improvement, the spatiotemporal deep graph neural network models, including MSI, STMeta, DCRNN, and ASTGCN, were used as basic models for the ablation study. The adjacency matrices generated by the above three strategies were input into the corresponding basic models for model training. The evaluation results were shown in Fig. 10. The results showed that the models with both algorithms achieved better forecasting performance than the others. Specifically, the models with suffix -MSI performed better than the models with suffix -OMSI, indicating that the trajectory enhancement algorithm (fixing the issue of insufficient interaction sampling in less crowded places) was helpful for achieving better

<table>
<thead>
<tr>
<th>Compared pairs</th>
<th>K-S statistics</th>
<th>p-values</th>
</tr>
</thead>
<tbody>
<tr>
<td>CDF-MSI &amp; STMeta</td>
<td>0.1808</td>
<td>p &lt; 0.001</td>
</tr>
<tr>
<td>CDF-MSI &amp; DCRNN</td>
<td>0.2173</td>
<td>p &lt; 0.001</td>
</tr>
<tr>
<td>CDF-MSI &amp; ASTGCN</td>
<td>0.0345</td>
<td>p &lt; 0.001</td>
</tr>
<tr>
<td>CDF-MSI &amp; LSTM</td>
<td>0.2270</td>
<td>p &lt; 0.001</td>
</tr>
<tr>
<td>CDF-MSI &amp; KNN</td>
<td>0.0829</td>
<td>p &lt; 0.001</td>
</tr>
<tr>
<td>CDF-MSI &amp; GBDT</td>
<td>0.0864</td>
<td>p &lt; 0.001</td>
</tr>
</tbody>
</table>

Fig. 8. Effect of crowd size on the RMSE.
forecasting performance. Both the models with suffix -MSI and -OMSI outperformed other models, indicating that the multi-order spatial interaction learning algorithm also contributed to the improvement in forecasting performance. These results demonstrated the advantage of the two algorithms proposed in this paper to a certain extent.

As for the trajectory enhancement algorithm, the 2nd-order random walk with historical movement interaction was used to generate simulated trajectories in this study. To test the similarity between the simulated trajectories and the real trajectories, a simulated trajectory dataset was generated. The number of generated trajectories originated from each place is equal to its average population count observed from the mobile phone data. The Pearson correlation was chosen as the evaluation metric, and the perspectives of average number of stay points per place, the median trajectory entropy per place, the crowd distribution, and the movement interaction matrix, were chosen to measure the similarity between the real trajectories and the simulated trajectories (Wang et al., 2019). The results were shown in Table 5. The correlation coefficients between the simulation trajectories and real trajectories in all four perspectives were over 0.8 and the correlation were statistically significant at the 0.01 level. A 2nd-order random walk with topological adjacency, a structural-similarity-based biased walk (Ribeiro et al., 2017), and a deep learning-based trajectory simulation algorithm LSTM-TrajGAN (Rao et al., 2020) were also conducted as the baselines. The coefficient values were lower than our proposed algorithm. These results indicated that the proposed algorithm can capture the movement spatial pattern well. However, it is worth

![Fig. 9. Effect of crowd variation diversity on the RMSE.](image)

![Fig. 10. Verification of the applicability of these two algorithms on performance improvement.](image)

<table>
<thead>
<tr>
<th>Simulated algorithm</th>
<th>Number of stay points</th>
<th>Trajectory entropy</th>
<th>Crowd distribution</th>
<th>Interaction matrix</th>
</tr>
</thead>
<tbody>
<tr>
<td>2nd-order – Movement</td>
<td>0.814**</td>
<td>0.899**</td>
<td>0.889**</td>
<td>0.903**</td>
</tr>
<tr>
<td>2nd-order – Topology</td>
<td>0.346**</td>
<td>0.555**</td>
<td>0.658**</td>
<td>0.606**</td>
</tr>
<tr>
<td>Structural-similarity-based</td>
<td>0.346**</td>
<td>0.538**</td>
<td>-0.158**</td>
<td>0.002**</td>
</tr>
<tr>
<td>LSTM-TrajGAN</td>
<td>-0.001</td>
<td>0.055**</td>
<td>0.041</td>
<td>0.011</td>
</tr>
</tbody>
</table>

** Correlation is significant at the 0.01 level.
noting that the simulation trajectories were still different from real trajectories. Therefore, we tried to find a balance between adding trajectories to address the sampling problem and reducing the noise. A model with simulation trajectories on all places was conducted for comparison. The RMSE, MAE, and StDev of this model were 8.951, 4.646, and 8.925, respectively, which was worse than those of our proposed method (as shown in Table 3). The ablation study results further demonstrated the effectiveness of our proposed trajectory enhancement algorithm. Furthermore, the performance difference between these two models is not that significant. This may be due to the fact that adding simulation trajectories in already crowded places has less effect on interaction modelling.

To further measure the multi-order spatial interaction effect on crowd distribution forecasting, a parameters analysis on the multi-order size and a spatial residual analysis were conducted. As shown in Fig. 11, the forecasting performance shows an overall trend of increasing and then decreasing with the increase in the multi-order interaction size and the best forecasting performance was achieved with the value of 9 (an RMSE of 8.885, MAE of 4.633, and standard deviation of error (StDev) of 8.884). This can be explained by the conjecture that a small size fails to capture the multi-order spatial interaction patterns, and a very large size results in too many places being considered, thus reducing the pertinence of modelling a specific place.

From the spatial perspective, the RMSE comparison between our proposed CDF-MSI method and the first-order interaction CDF-I method in each place was shown in Fig. 12. The places where the RMSE of CDF-I is greater than that of CDF-MSI were labelled in red, and the opposite parts were labelled in blue. Fig. 12(a) shows the overall comparison result across the country. It suggests that considering multi-order spatial interaction can improve forecasting performance on most places (CDF-I was significantly better than CDF-MSI on only 8.82 % of the places). The places where CDF-I performs better distributed sporadically. Combined with the local individual movement pattern, this may be explained by the fact that the lower frequency of movement among places of local residents reduces the impact of multi-order spatial interactions on the near real-time crowd distribution forecasting. Considering the greater application value of fine-grained crowd distribution forecasting in crowded areas, we selected region Dakar (where the capital of Senegal is located, marked as ①) and region Diourbel (one of the central core regions, marked as ②) to further analyse the differences in forecasting performance. It can be seen in Fig. 12(b) and 12(c) that our proposed method has achieved an overall advantage (CDF-I was significantly better than CDF-MSI on only 9.96 % and 3.97 % of places in Dakar and Diourbel, respectively), which demonstrated the superiority of considering the multi-order interaction in crowd distribution forecasting.

5. Discussion

5.1. Attempts at trajectory enhancement in interaction pattern learning

“How much data is big enough” is a typical but always overlooked problem in big data applications (Wang et al., 2017; Splinter et al., 2013). In these applications, we usually regard the acquired big data (sample) as a true reflection of the population, ignoring the impact of the chosen sampling strategy (e.g., the number of users and the time period) on the population characteristics. Especially in location-based transportation research, given the spatial heterogeneity phenomenon, sampling strategy differences can be particularly prominent in areas with sparse data. To explore the effect of crowd size on the sampling result, we randomly sampled 50 % of the trajectories from the dataset and generated the movement interaction matrixes of the post-sampling data and the pre-sampling data respectively. The experimental results showed that the correlation between the pre-sampling interaction matrix and the post-sampling interaction matrix in the crowded places was 0.93, while the correlation between the interaction matrix before and after sampling in the less crowded places was only 0.87. It indicated that the differences were mainly observed in the less crowded places. This situation exacerbated our concern with respect to modelling the interactions among the less crowded places using raw sample trajectory data. Data augmentation, which refers to methods for constructing sampling algorithms via the introduction of unobserved data, has been widely used in the fields such as language translation, image classification, and recommendation systems (Chen et al., 2019a,b; Van Dyk and Meng, 2001; Wang and Perez, 2017; Xie et al., 2020; Wang et al., 2020). For example, Chen et al. (2019) enriched the user-network structure and employed node2vec to alleviate the data sparsity problem in recommender system. Wang et al. (2017) explored and compared multiple solutions to the problem of data augmentation in image classification. These studies implicated the potential of data augmentation in solving data sparsity problems. The trajectory enhancement algorithm was an instance of data augmentation in movement interaction pattern learning and an attempt to mitigate the insufficient sampling issue. Further explorations, such as more reasonable sampling expansion strategies or more diverse data, would contribute to a more comprehensive understanding of human movements and spatial interaction patterns.

5.2. The application of embedding learning techniques for multi-order spatial interaction learning

As the movements of individuals in space are continuous, the crowd distribution in a place is influenced by the surrounding places to a certain extent, thus reflecting the “coevolution” phenomenon. How to measure the spatial scope and intensity of this influence among different places has become an important topic for improving the accuracy of crowd distribution forecasting. Essentially, the influence among places originates from individual movements. Therefore, the inherent influence among places can be extracted from massive individual trajectories (Li et al., 2021; Liu et al., 2020; Liu et al., 2017).

A trajectory can be considered the combination of a series of stops and movements, which can be represented as a stop sequence such as “location$_{1}$, location$_{2}$, ..., location$_{n}$$\$”. This means that the crowd distribution pattern of location$_{n}$ is influenced not only by location$_{n-1}$ and location$_{n+1}$ but also by locations from location$_{n-g}$ to location$_{n+g}$ (where g indicates the spatial scope of the influence mentioned in the above paragraph). This influence among multiple places was defined as a multi-order spatial interaction in this study.
The text-like structures of trajectories provide an efficient way to model the multi-order interaction among places using the embedding learning technique. Each location in the trajectory corresponding to the text structure "word_1, word_2, ..., word_k" was analogous to a word in a sentence. Therefore, the multi-order spatial interactions can be regarded as the text similarity, which can be captured with embedding learning techniques. A higher multi-order spatial interaction intensity indicates that two places more frequently co-occur or possess common contextual neighbours in the trajectories, which also reflects higher spatial influence.

5.3. Limitations and future work

Several limitations of this study are worth noting and further exploring in future work. First, in the current CDF-MSI method, the 2nd-order random walk algorithm was used to generate simulated trajectories for trajectory data enhancement. Although this algorithm considered the historical movement pattern for transition weight matrix generation, the generated trajectories were still different from the real trajectories. This affected the accuracy and reliability of the spatial interaction modelling results to a certain extent. Advanced trajectory simulation strategies and other data expansion algorithms such as generative adversarial neural networks (Choi et al. 2021) and mobility Markov chain (Gambs et al. 2012) may further improve the forecasting performance. Second, the original word embedding model word2vec was applied in the proposed CDF-MSI method. This model can effectively extract the co-occurrence relationships and common context relationships among texts, which have been used in the explorations of road network structure (Chen et al., 2021; Wu et al., 2020; Wang et al., 2019). In our method, the multi-order spatial interactions among contextual non-adjacent places were modelled with this model using enhanced trajectories to capture the spatial correlations more comprehensively, thus improving the accuracy and stability of crowd distribution forecasting. It is worth noting that the implementation process in this paper has similarities with Node2Vec (Grover & Leskovec, 2016), but there are two differences. The initial weight matrix used in random walk of our method was based on the historical movement interaction, and the corresponding initial weight matrix of the Node2Vec was based on the topological adjacency. Besides, the Node2Vec method generates the same number of trajectories at each node, while our method does not. These made the learned edge weight matrix somewhat different. We also compared the forecasting performance based on our algorithm and the Node2Vec algorithm. The RMSE, MAE, and StDev of the Node2Vec based method were 9.528, 4.974, and 9.526, respectively, which was worse than those of our proposed method (8.885 on...
RMSE, 4.633 on MAE, and 8.884 on StDev). Other advanced embedding learning techniques, such as BERT-flow and SimCSE, may help improve forecasting performance in future work (Su et al., 2021; Gao et al., 2021; Chen et al., 2021). In addition, the built environment can constrain and influence the movement behaviours of crowds (Tu et al., 2020). Five dimensions of the built environment (density, diversity, design, distance, and destination) were investigated for their effects on crowd distribution dynamics (Wu et al., 2018; Higgins & Kanaroglou, 2016). The consideration of the influence of the built environment can be an extension of crowd distribution forecasting methods. Moreover, it is worth noting that the network parameter has a great impact on forecasting performance. When increasing the number of GCN and LSTM layers from one to three, the RMSE of CDF-MSI model decreased from 8.885 to 8.589. Considering that the compared spatiotemporal graph-based models STMeta and ASTGCN typically used one spatial layer and one temporal layer for model training, we used one GCN layer and one LSTM layer in the case study to make the validation more comparable and less time consuming. The forecasting performance can be further improved by designing more complex network structures in future studies. Finally, in this study, the numbers of calls and mobile users were used to estimate the dynamic crowd distribution. Although linear relationships between crowd distribution and these two indicators have been demonstrated (Cheng et al., 2020; Kang et al., 2012), the potential impacts of sampling biases and uncertainty are of concern. Our future work will focus on solving these issues.

6. Conclusion

This study proposed a novel crowd distribution forecasting method considering the multi-order spatial interactions along different places using mobile phone data. We focus on two prevalent but not yet properly addressed limitations in current relevant studies: the insufficient interaction modelling in less crowded places caused by the lack of sampling design, and ignorance of multi-order spatial interactions among contextual non-adjacent places. To mitigate the influence of these issues, we applied a weighted random walk algorithm to generate simulated trajectories to improve the accuracy and robustness of the interaction characterizations in less crowded places. With the enhanced trajectories, we adopted an embedding learning algorithm to model the multi-order spatial interactions among contextual non-adjacent places. A hybrid forecasting model was then constructed that combines a GCN and an RNN for modelling the spatiotemporal pattern of crowd distribution variations. Our proposed method was verified using a real-world mobile phone dataset in a country. The results indicate that both the multi-order spatial interactions and the trajectory enhancement algorithm helped improve the crowd distribution forecasting performance. The CDF-MSI method also outperformed other baseline methods in terms of the RMSE, MAE, and StDev of the forecasting error.

This study provides an effective method to forecast fine-grained crowd distribution. The method allows us to capture future crowd distribution variations across space, which technically supports for transportation applications such as traffic optimization, emergency evacuation, and cell base station operation. In addition, crowd distribution variation patterns can help reveal the patterns of human movements, thus enriching the theory and practices related to human mobility studies.

CRediT authorship contribution statement

Mingxiao Li: Conceptualization, Methodology, Formal analysis, Visualization, Writing – original draft, Project administration. Song Gao: Conceptualization, Data curation, Investigation, Writing – review & editing. Peiyuan Qiu: Resources, Writing – review & editing. Wei Tu: Conceptualization, Resources, Writing – review & editing, Funding acquisition, Project administration. Feng Lu: Supervision, Resources, Writing – review & editing, Funding acquisition. Tianhong Zhao: Visualization, Writing – review & editing. Qingquan Li: Supervision, Resources, Writing – review & editing, Funding acquisition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary material

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